

Dynamics Chapter Problems
10-19 and 26-31

10) Use $\vec{F} = m\vec{a}$

$$\vec{F} = 50 \text{ kg} \cdot 1.5 \frac{\text{m}}{\text{s}^2} = 75 \text{ kg} \frac{\text{m}}{\text{s}^2} = \boxed{75 \text{ N}}$$

11) $\vec{F} = m\vec{a}$, so $m = \frac{\vec{F}}{\vec{a}} = \frac{10000 \text{ N} \frac{\text{kgm}}{\text{s}^2}}{5.5 \frac{\text{m}}{\text{s}^2}} = \boxed{1818 \text{ kg}}$

12) $\vec{F} = m\vec{a}$, so $\vec{a} = \frac{\vec{F}}{m} = \frac{235 \text{ kg} \frac{\text{m}}{\text{s}^2}}{40 \text{ kg}} = \boxed{5.9 \frac{\text{m}}{\text{s}^2}}$

13) $\vec{F} = m\vec{a}$

Knowns are $m = 45 \text{ kg}$ $v_f = 12 \frac{\text{m}}{\text{s}}$ $v_i = 0 \frac{\text{m}}{\text{s}}$ $x_i = 0 \text{ m}$

~~Use $x_f = x_0 + v_0 t + \frac{1}{2} a t^2$~~

$x_f = 20 \text{ m}$

Need to find a , so use ~~$v_f^2 = v_i^2 + 2a(x_f - x_i)$~~

$v_f^2 = v_0^2 + 2a(x - x_0)$ to find a

$$v_f^2 - v_0^2 = 2a(x - x_0)$$

$$a = \frac{1}{2} \left(\frac{v_f^2 - v_0^2}{x - x_0} \right) = \frac{1}{2} \left(\frac{(12 \frac{\text{m}}{\text{s}})^2 - (0 \frac{\text{m}}{\text{s}})^2}{20 \text{ m} - 0 \text{ m}} \right) = \frac{1}{2} \left(\frac{144 \frac{\text{m}^2}{\text{s}^2}}{20 \text{ m}} \right)$$

$$a = 3.6 \frac{\text{m}}{\text{s}^2}$$

Now,
Use $\vec{F} = m\vec{a}$ $\vec{F} = 45 \text{ kg} \cdot 3.6 \frac{\text{m}}{\text{s}^2} = \boxed{162 \text{ N}}$

(14) Knowns: $\vec{F} = 3000 \text{ N}$ $m = 1700 \text{ kg}$
wants to know time

$$\begin{array}{l} \uparrow \\ 15 \text{ m} = x_f \\ x_0 = 0 \text{ m} \end{array}$$

First, use $\vec{F} = m\vec{a}$ to solve for \vec{a} .

$$\vec{a} = \frac{\vec{F}}{m} = \frac{3000 \text{ kg} \frac{\text{m}}{\text{s}^2}}{1700 \text{ kg}} = 2.5 \frac{\text{m}}{\text{s}^2}$$

Now, use $x_f = x_0 + v_0 t + \frac{1}{2} a t^2$ to find t

$v_0 = 0$ and $x_0 = 0$, so

$$x_f = \frac{1}{2} a t^2 \quad \text{solve for } t$$

$$\sqrt{\frac{2x_f}{a}} = t = \sqrt{\frac{2 \cdot 15 \text{ m}}{2.5 \frac{\text{m}}{\text{s}^2}}} = 3.55$$

(15) Knowns: $57 \text{ kg} = m$ and $a = 9.8 \frac{\text{m}}{\text{s}^2}$
wants force

Use $\vec{F} = m \cdot \vec{a}$ to find force

$$\vec{F} = 57 \text{ kg} \cdot 9.8 \frac{\text{m}}{\text{s}^2} = 558.6 \text{ N}$$

(16) Knowns: $\vec{F} = 34 \text{ N}$ $\vec{a} = 2.5 \frac{\text{m}}{\text{s}^2}$

Find mass. Use $\vec{F} = m \cdot \vec{a}$, so

$$m = \frac{\vec{F}}{\vec{a}} = \frac{34 \text{ kg} \frac{\text{m}}{\text{s}^2}}{2.5 \frac{\text{m}}{\text{s}^2}} = 13.6 \text{ kg}$$

(17) Knowns $\vec{F} = 775 \text{ N}$ $\vec{a} = 3.0 \frac{\text{m}}{\text{s}^2}$

Unknown is mass

Use $\vec{F} = m \cdot \vec{a}$, so $m = \frac{\vec{F}}{\vec{a}} = \frac{775 \text{ N}}{3.0 \frac{\text{m}}{\text{s}^2}} =$

75 kg

(18) Given $m = 4 \text{ kg}$ $t = 0.5 \text{ s}$ $v_{f1} = 10 \frac{\text{m}}{\text{s}}$

Final \vec{F}_{net} , need to find \vec{a} , so use

$$v_f = v_0 + at \quad \therefore v_f - v_0 = at$$

$$a = \frac{v_f - v_0}{t} = \frac{(0 \frac{\text{m}}{\text{s}} - 10 \frac{\text{m}}{\text{s}})}{0.5 \text{ s}} = -20 \frac{\text{m}}{\text{s}^2}$$

Now, use $\vec{F} = m \cdot \vec{a}$

$$\vec{F} = 4 \text{ kg} \cdot -20 \frac{\text{m}}{\text{s}^2} = -80 \text{ N}$$

(19) Knowns $m = 0.18 \text{ kg}$ $\vec{F} = 0.5 \text{ N}$

First, find \vec{a}

$$\vec{F} = m\vec{a}, \text{ so } \vec{a} = \frac{\vec{F}}{m} =$$

$$\vec{a} = \frac{0.5 \text{ N}}{0.18 \text{ kg}} = 2.8 \frac{\text{m}}{\text{s}^2}$$

$$\vec{v} = v_0 + at = 0 \frac{\text{m}}{\text{s}} + (2.8 \frac{\text{m}}{\text{s}^2} \cdot 5 \text{ s}) = 14 \frac{\text{m}}{\text{s}}$$

$$x_f = x_0 + v_0 t + \frac{1}{2} at^2 = \frac{1}{2} at^2 = \frac{1}{2} \cdot 2.8 \frac{\text{m}}{\text{s}^2} (5 \text{ s})^2 = 35 \text{ m}$$

(26) $\vec{F} = m \cdot \vec{a}$ $m = \frac{\vec{F}}{\vec{a}} = \frac{270 \text{ Kg} \frac{\text{m}}{\text{s}^2}}{9.8 \frac{\text{m}}{\text{s}^2}} =$

Knowns: $\vec{F} = 270 \text{ N}$
 $\vec{a} = 9.8 \frac{\text{m}}{\text{s}^2}$

27.6 Kg

(27) Weight = $\vec{F} = m \vec{g}$

Knowns: $m = 60 \text{ Kg}$, $\vec{a} = 9.8 \frac{\text{m}}{\text{s}^2}$

Find \vec{F}

$\vec{F} = 60 \text{ Kg} \cdot 9.8 \frac{\text{m}}{\text{s}^2} = 588 \text{ N}$

(28) $\vec{F}_{\text{mars}} = 17 \text{ N}$ $\vec{g}_{\text{mars}} = 3.8 \frac{\text{m}}{\text{s}^2}$

Find mass using $\vec{F} = m \vec{g}$

$m = \frac{\vec{F}}{\vec{g}} = \frac{17 \text{ Kg} \frac{\text{m}}{\text{s}^2}}{3.8 \frac{\text{m}}{\text{s}^2}} = 4.5 \text{ Kg}$

Weight on Earth = $4.5 \text{ Kg} \cdot 9.8 \frac{\text{m}}{\text{s}^2} = 44.1 \text{ N}$

Weight on Moon = $4.5 \text{ Kg} \cdot 1.6 \frac{\text{m}}{\text{s}^2} = 7.2 \text{ N}$

Mass does not change. Only weight does!

$$(29) \text{ weight} = \vec{F}_g = m \cdot \vec{a} =$$

$$Xg \cdot 9.8 \frac{m}{s^2} =$$

$$0.002 \text{ Kg} \cdot 9.8 \frac{m}{s^2} = 0.02 \text{ N}$$

$$(30) \text{ Known: } \vec{F}_g = 330 \text{ N} \cdot \vec{a} = 9.8 \frac{m}{s^2}$$

Use $\vec{F} = m\vec{a}$, solve for m

$$m = \frac{\vec{F}}{\vec{a}} = \frac{330 \text{ Kg} \frac{m}{s^2}}{9.8 \frac{m}{s^2}} = 33.7 \text{ Kg}$$

$$(31) \text{ Known: } m = 836 \text{ Kg} \quad g_{\text{mars}} = 3.8 \frac{m}{s^2}$$

weight on Mars:

$$\vec{F}_{\text{mars}} = 836 \text{ Kg} \cdot 3.8 \frac{m}{s^2} = 3177 \text{ N}$$

weight on Earth:

$$\vec{F}_{\text{earth}} = 836 \text{ Kg} \cdot 9.8 \frac{m}{s^2} = 8193 \text{ N}$$