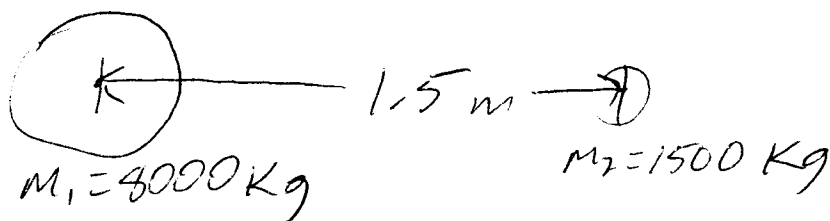


# Gravitation Problems 6-15

6

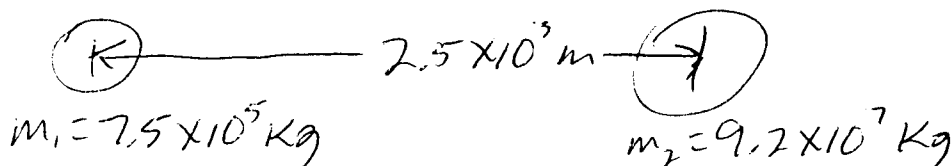


what is  $F_g$ ?

$$F_g = \frac{G m_1 m_2}{r^2} = \frac{(6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}) \cdot 8000 \text{ kg} \cdot 1500 \text{ kg}}{(1.5 \text{ m})^2}$$

$$= 3.56 \times 10^{-4} \text{ N}$$

7



$$F_g = \frac{G m_1 m_2}{r^2} = \frac{(6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}) \cdot 7.5 \times 10^5 \text{ kg} \cdot 9.2 \times 10^7 \text{ kg}}{(2.5 \times 10^3 \text{ m})^2} =$$

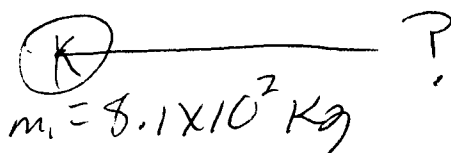
~~$$F_g = 1.9 \times 10^{-3} \text{ N}$$~~

$$F_g = 7.36 \times 10^{-4} \text{ N}$$

$$\vec{F}_{2on1} = 1.9 \times 10^{-3} \text{ N}$$

$$\vec{F}_{1on2} = 1.9 \times 10^{-3} \text{ N}$$

8



$$m_2 = 4.5 \times 10^4 \text{ kg}$$

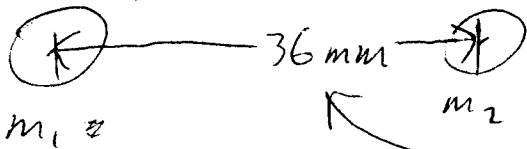
$$r = 113.1 \text{ m}$$

$$F = \frac{G m_1 m_2}{r^2}$$

Solve for  $r$   $\therefore r^2 \cdot F = G m_1 m_2$

$$r^2 = \frac{G m_1 m_2}{F} \therefore r = \sqrt{\frac{G m_1 m_2}{F}} = \sqrt{\frac{6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2} \cdot 8.1 \times 10^2 \text{ kg} \cdot 4.5 \times 10^4 \text{ kg}}{1.9 \times 10^{-3} \text{ N}}}$$

$$\vec{F}_{2on1} = 85\text{ N} \quad \leftarrow \vec{F}_{1on2} = 85\text{ N}$$



make sure to convert to m.

$$m_1 = m_2 \quad \text{what are masses?} \quad 36\text{ mm} \left( \frac{1\text{ m}}{1000\text{ mm}} \right) =$$

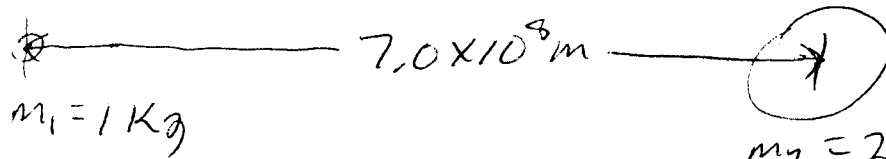
$$0.036\text{ m}$$

$$F_g = \frac{G m_1 m_2}{r^2} \quad \text{Since } m_1 = m_2, \text{ we can simplify as } m^2$$

$$F_g = \frac{G m^2}{r^2} \quad \therefore m^2 = \frac{F_g \cdot r^2}{G} \quad \therefore m = \sqrt{\frac{F_g \cdot r^2}{G}}$$

$$m = \sqrt{\frac{85 \frac{\text{kgm}}{\text{s}^2} \cdot (0.036\text{ m})^2}{6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}}} = 40640\text{ kg}$$

10



$$m_1 = 1\text{ kg}$$

$$m_2 = 2.0 \times 10^{30}\text{ kg}$$

a) what is magnitude of force on smaller object?

$$F_g = \frac{G m_1 m_2}{r^2} = \frac{6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2} \cdot 1\text{ kg} \cdot 2.0 \times 10^{30}\text{ kg}}{(7.0 \times 10^8\text{ m})^2}$$

$$= 272\text{ N}$$

b) what is magnitude of force on larger object?

According to Newton's 3rd Law, the force of mass 1 on mass 2 is equal to in magnitude, but opposite in direction to the force of mass 2 on mass 1.

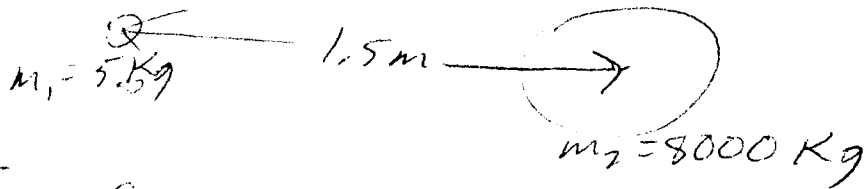
$$\text{So, } F = 272\text{ N}$$

$$c) a_1 = \frac{F}{m_1} = \frac{272 \frac{\text{kgm}}{\text{s}^2}}{1\text{ kg}} = 272 \frac{\text{m}}{\text{s}^2}$$

$$d) a_2 = \frac{F}{m_2} = \frac{272 \frac{\text{kgm}}{\text{s}^2}}{2.0 \times 10^{30}\text{ kg}} = 1.36 \times 10^{-28} \frac{\text{m}}{\text{s}^2}$$

2

(11)

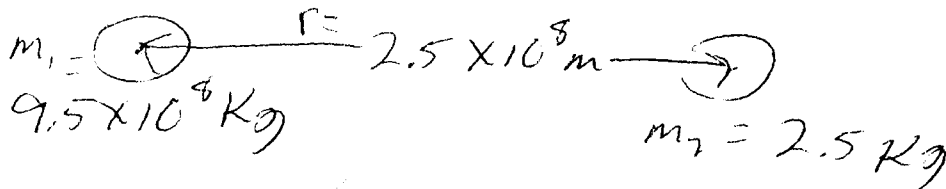


$$F_g = \frac{G m_1 m_2}{r^2} = \frac{(6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}) \cdot 5.0 \text{ kg} \cdot 8000 \text{ kg}}{(1.5 \text{ m})^2}$$

~~$$F_g = 7.11 \times 10^5 \text{ N}$$~~

$$F_g = 1.2 \times 10^{-6} \text{ N}$$

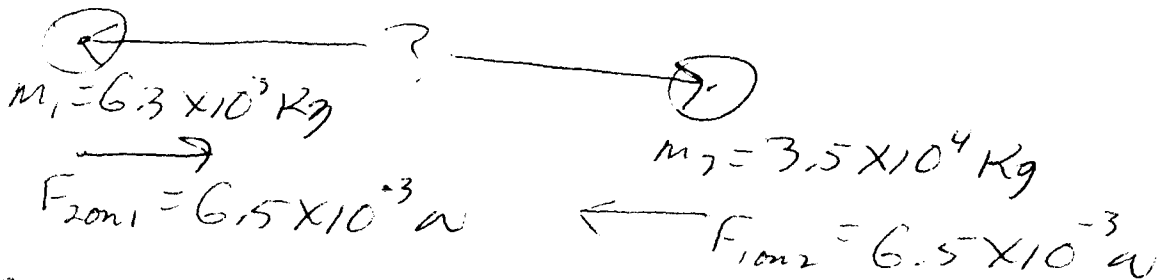
(12)



$$F_g = \frac{G m_1 m_2}{r^2} = \frac{(6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}) \cdot 9.5 \times 10^8 \text{ kg} \cdot 2.5 \text{ kg}}{(2.5 \times 10^8 \text{ m})^2}$$

$$F_g = 2.5 \times 10^{-18} \text{ N}$$

(13)



$$F_g = \frac{G m_1 m_2}{r^2} \text{ what is } r? \quad F_g \cdot r^2 = G m_1 m_2$$

$$r = \sqrt{\frac{6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2} \cdot 6.3 \times 10^3 \text{ kg} \cdot 3.5 \times 10^4 \text{ kg}}{6.5 \times 10^{-3} \text{ N}}} = \frac{G m_1 m_2}{F_g}$$

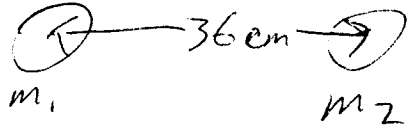
$$r = \sqrt{\frac{G m_1 m_2}{F_g}} =$$

$$r = 1.5 \text{ m}$$

(14)

$$F_{2on1} = 25 \text{ N}$$

$$F_{1on2} = 25 \text{ N}$$



Convert 36 cm to m.

$$36 \text{ cm} \left| \frac{1 \text{ m}}{100 \text{ cm}} \right. =$$

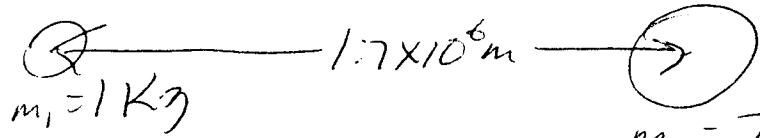
since  $m_1, m_2$  are equal:

$$F_g = \frac{G m_1 m_2}{r^2} \therefore F_g = \frac{G m^2}{r^2}$$

$$m^2 = \frac{F_g r^2}{G} = \frac{(25 \text{ N} \cdot (0.36 \text{ m})^2)}{6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}}$$

$$m = 2.2 \times 10^5 \text{ kg}$$

(15)



$$m_1 = 1 \text{ kg}$$

$$m_2 = 7.4 \times 10^{22} \text{ kg}$$

a) what is force on  $m_1$ ?

$$F_g = \frac{G m_1 m_2}{r^2} = \frac{(6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2} \cdot 1 \text{ kg} \cdot 7.4 \times 10^{22} \text{ kg})}{(1.7 \times 10^6 \text{ m})^2}$$

$$F_g = 1.7 \text{ N}$$

b) Because of Newton's 3rd Law, Force on  $m_2$  is also 1.7 N.

$$c) a_1 = \frac{F}{m_1} = \frac{1.7 \text{ N}}{1 \text{ kg}} = 1.7 \frac{\text{m}}{\text{s}^2}$$

$$d) a_2 = \frac{F}{m_2} = \frac{1.7 \frac{\text{kg} \cdot \text{m}}{\text{s}^2}}{7.4 \times 10^{22} \text{ kg}} = 2.3 \times 10^{-23} \frac{\text{m}}{\text{s}^2}$$

(4)