

Kinematics Problems 83-88

$$83) V_f^2 = V_0^2 + 2a(x - x_0)$$

$$\cancel{a} = V_f^2 - V_0^2 = 2a(x - x_0) \therefore \frac{V_f^2 - V_0^2}{(x - x_0) \cdot 2} = a$$

$$a = \frac{1}{2} \left(\frac{(85 \frac{m}{s})^2 - (0 \frac{m}{s})^2}{(36 m - 0 m)} \right) = \frac{1}{2} \left(\frac{7225 \frac{m^2}{s^2}}{36 m} \right) = \boxed{100.3 \frac{m}{s^2}}$$

$$84) V_f^2 = V_0^2 + 2a(x - x_0)$$

$$V_f^2 - V_0^2 = 2a(x) \therefore x = \frac{V_f^2 - V_0^2}{2a}$$

$$x = \frac{0 \frac{m^2}{s} - 54 \frac{m^2}{s}}{2 \cdot -6.8 \frac{m}{s^2}} = \frac{-2916 \frac{m^2}{s^2}}{-13.6 \frac{m}{s^2}} = \boxed{214 m}$$

$$85) V_f = ? \quad V_0 = 0 \frac{m}{s} \quad x_0 = 0 m \quad x_f = -32 m$$

$$V_f^2 = V_0^2 + 2a(x - x_0)$$

$$V_f = \sqrt{V_0^2 + 2a(x - x_0)} = \sqrt{0^2 + 2a(+32 m - 0 m)}$$

$$= \sqrt{2 \cdot -9.8 \frac{m}{s^2} (-32 m)} = \sqrt{627.2 \frac{m^2}{s^2}}$$

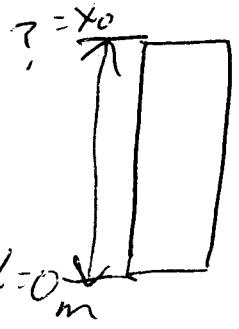
$$\boxed{V_f = -25 \frac{m}{s}}$$

$$86) V_f^2 = V_0^2 + 2a(x - x_0)$$

$$V_f^2 - V_0^2 = 2a(x - x_0)$$

$$V_f = -31 \frac{m}{s}$$

$$V_0 = 0 \frac{m}{s}$$



$$\frac{V_f^2 - V_0^2}{2a} = x - x_0 \quad \therefore -x_0 = \left(\frac{V_f^2 - V_0^2}{2a} \right) - x$$

$$-x_0 = \frac{\left(-31 \frac{m}{s} \right)^2 - 0 \frac{m^2}{s^2}}{2 \cdot -9.8 \frac{m}{s^2}} - 0$$

$$-x_0 = \frac{961 \frac{m^2}{s^2}}{-19.6 \frac{m}{s^2}} = -49 \text{ m}$$

$$\boxed{x_0 = 49 \text{ m}}$$

$$87) \quad x = 1.3 \text{ m} \quad a = -9.8 \frac{m}{s^2} \quad V_0 = ?$$

$$x = 0 \text{ m}$$

$$V_f = 0 \frac{m}{s}$$

$$V_f^2 - V_0^2 = 2a(x - x_0)$$

$$-V_0^2 = 2a(x - x_0) - V_f^2$$

$$V_0 = \sqrt{2a(x - x_0) - V_f^2} =$$

$$V_0 = \sqrt{2 \cdot -9.8 \frac{m}{s^2} (1.3 \text{ m} - 0 \text{ m}) - \left(0 \frac{m}{s} \right)^2}$$

$$V_0 = \sqrt{2 \cdot -12.74 \frac{m^2}{s^2}} = \boxed{5 \frac{m}{s}}$$

(2)

88) $0.45 \text{ m} = x$ $V_f = 0 \frac{\text{m}}{\text{s}}$ assume $V_f = V_0$ here in opposite direction.

$x = 0$ $V_0 = ?$

$V_i = ?$

$V_f = 0 \frac{\text{m}}{\text{s}}$

$a = -9.8 \frac{\text{m}}{\text{s}^2}$

$$V_f^2 - V_0^2 = 2a(x - x_0)$$

$$-V_0^2 = 2a(x - x_0) - V_f^2$$

$$V_0^2 = -(2a(x - x_0) - V_f^2)$$

$$V_0 = \sqrt{2a(x - x_0) - V_f^2}$$

$$V_0 = \sqrt{2 \cdot -9.8 \frac{\text{m}}{\text{s}^2} (0.45 \text{ m} - 0 \text{ m}) - (0 \frac{\text{m}}{\text{s}})^2}$$

$$V_0 = \sqrt{2 \cdot -9.8 \frac{\text{m}}{\text{s}^2} \cdot 0.45 \text{ m}}$$

$$V_0 = \sqrt{8.82 \frac{\text{m}^2}{\text{s}^2}}$$

$$V_f = V_0 = -2.97 \frac{\text{m}}{\text{s}}$$